

# Refinements of Hilbert's Inequality Involving the Laplace Transform\*

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Received July 4, 2007, Accepted August 1, 2008.

## Abstract

In this paper generalizations of Peachey's results which refine some known Hilbert's inequalities in the sense that they interpolate Lebesgue norms of the Laplace transforms of the functions involved in the inequalities are obtained. Cases of conjugate and non-conjugate exponents are considered.

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\*2000 *Mathematics Subject Classification.* 26D15.

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**Keywords and Phrases:** *Hilbert's inequality, Conjugate exponents, Non-conjugate exponents, The Laplace transform, The beta function, The gamma function.*